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# AP Statistics <u>CHAPTER 19</u> Confidence Intervals for Proportions

## - Confidence Intervals:

A confidence interval is an interval estimate of a population parameter. Instead of estimating the parameter by a single value, an interval likely to include the parameter is given.

# **Constructing Confidence Intervals**

### - Check Assumptions and Conditions

All statistical models have assumptions. In order to determine the appropriate model, we must determine the plausibility of an assumption by checking a related condition.

- Plausible Independence Condition: Is it possible that the data values could affect each other?
- <u>Randomization Condition</u>: Were the data sampled at random or generated from a properly randomized experiment? Proper randomized data can ensure independence.
- ✓ <u>10% Condition</u>: Does the sample exceed 10% of the population? If so, the sample changes quite drastically which indicates that Normal model may no longer be appropriate.
- ✓ <u>Success/Failure Condition</u>: Are there at least 10 "successes" and 10 "failures"? The sample must be large enough to make the sampling model for the samples proportions approximately Normal.

#### - Mechanics

Find the standard error. [It is called the Standard error because we don't know the population proportion ( p ), only the observed proportion (  $\hat{p}$  )] -- (SE)

Find the margin of error. We could informally use 2 for our critical value, but 1.96 is more accurate. - (ME)

Write the Confidence interval. [Ex. n ± ME or (0.344, 0.546)]

#### - Conclusion

Interpret the confidence interval in the proper context. [Ex: I am 95% confident that between 34.4% and 54.6% of Americans read books on a weekly basis]

(SE) Standard error 
$$=\sqrt{rac{p(1-p)}{n}}$$
 (ME) Margin of Error = z\*(SE)



Normal Model